

The Horse Raced Past: Gardenpath Processing in Dynamical Systems

28.09.2011

Ninth International Tbilisi Symposium on Language,
Logic and Computation
Kutaisi, Georgia

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+

the

horse

raced

past

the

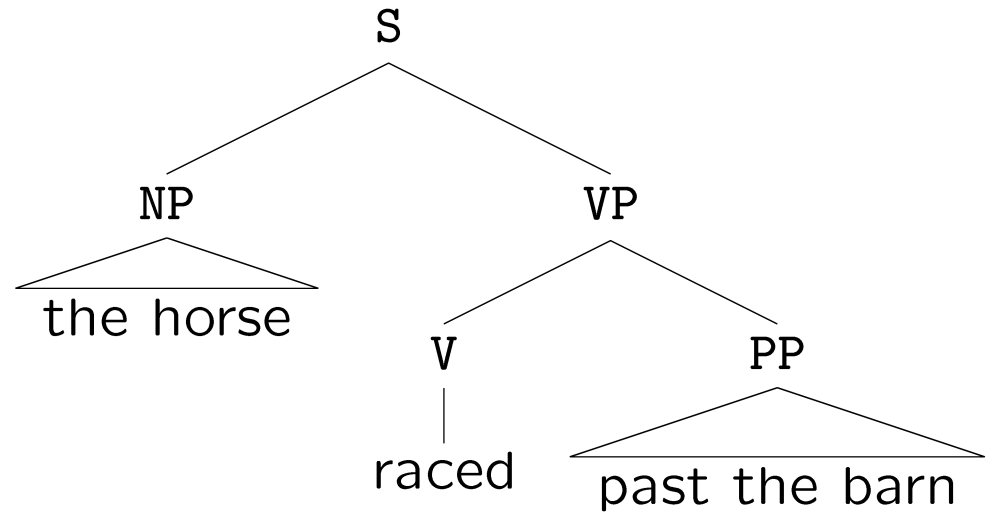
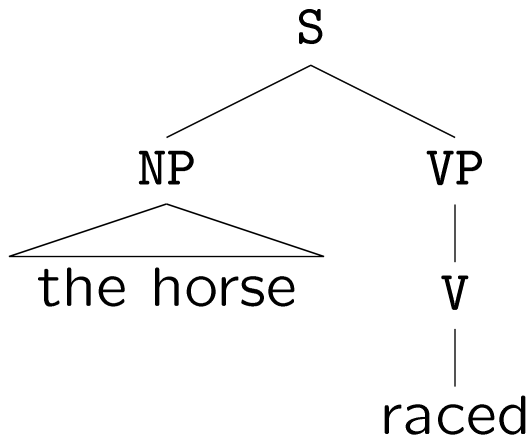
barn

fell.

Gardenpath Sentences



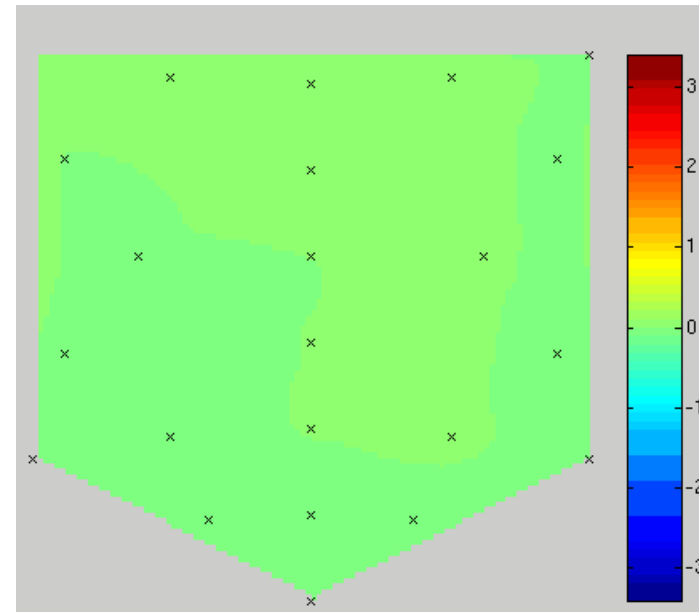
Gardenpath Theory



late closure

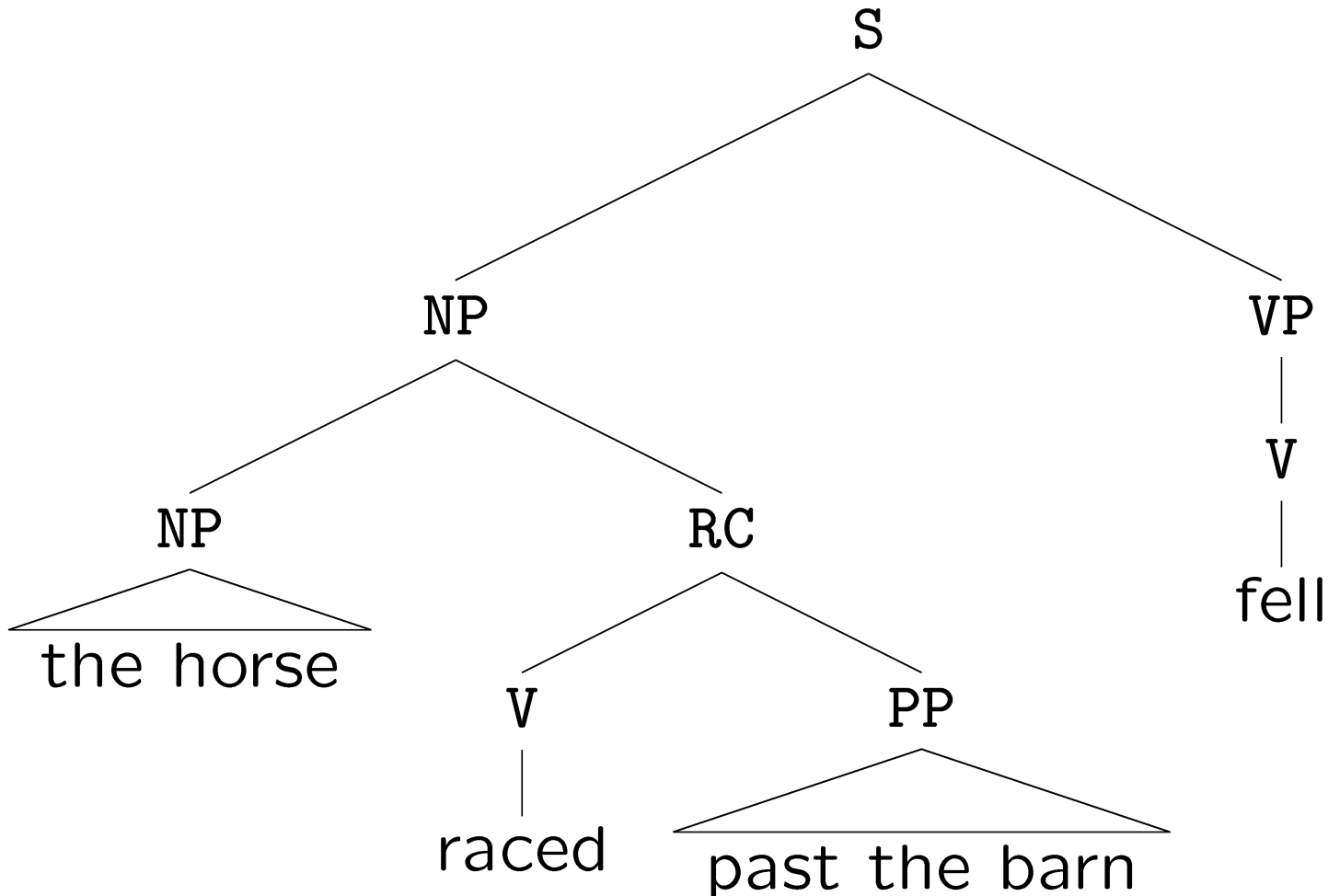
Experimental Findings

- Self-paced reading: **slowing down**
- Eye-tracking: **regressions, longer fixations**
- Event-related brain potentials: **P600**

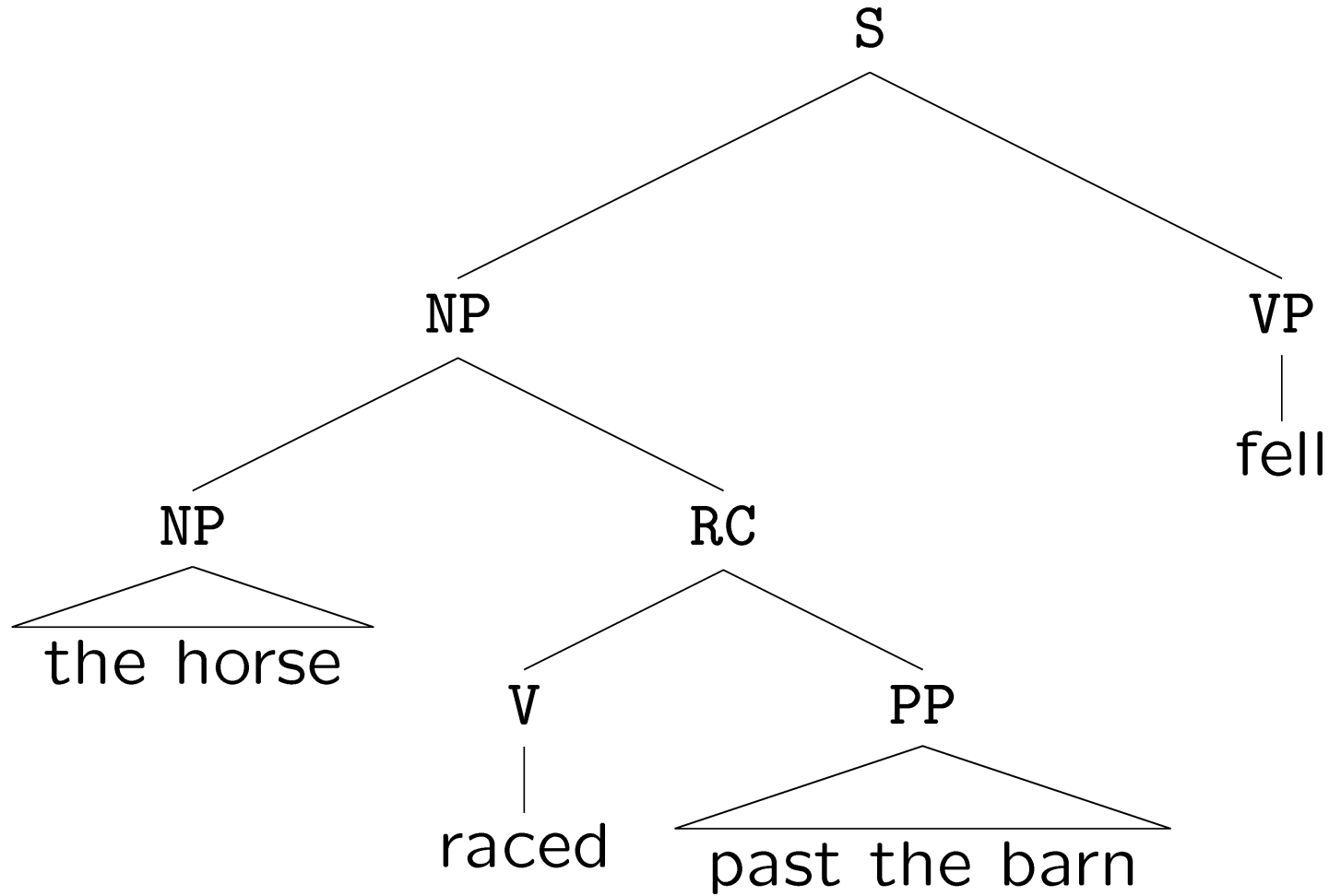
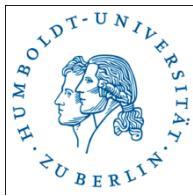


beim Graben et al. (2008)

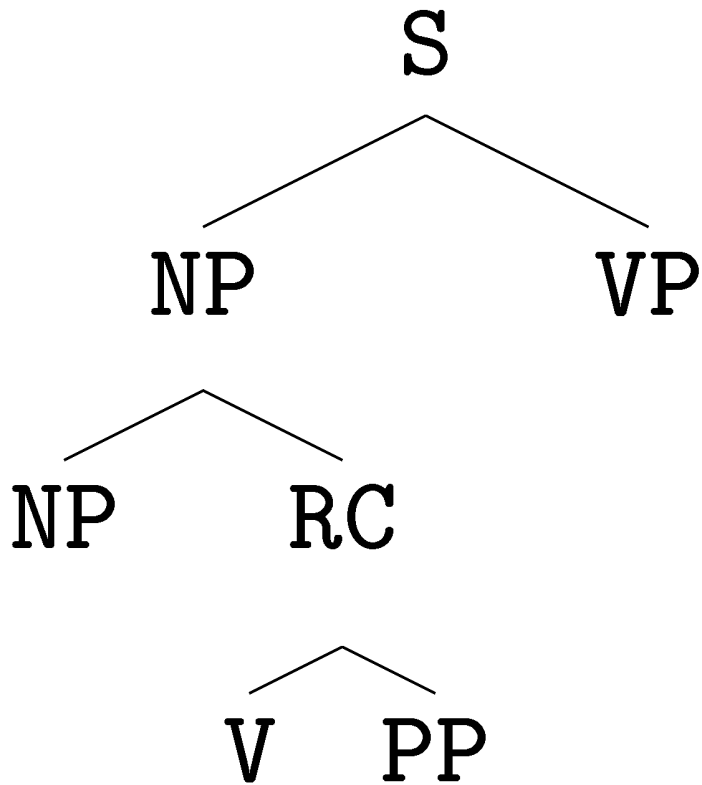
Reduced Relative



Simplified



Context-Free Grammars



$S \rightarrow NP \ VP.$

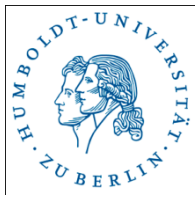
$NP \rightarrow NP \ RC.$

$RC \rightarrow V \ . \ PP$

$S \rightarrow NP \ . \ VP$

$VP \rightarrow V \ . \ PP$

Generalized Left-Corner Parser

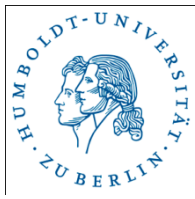


The horse raced past the barn fell.

1

| | | | | |
|-------|-----------|-------|---------------|------|
| stack | | | | |
| input | the horse | raced | past the barn | fell |

Generalized Left-Corner Parser



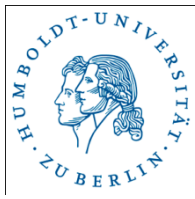
The horse raced past the barn fell.

| | | | | | |
|---|-------|-----------|-------|---------------|------|
| 1 | stack | | | | |
| | input | the horse | raced | past the barn | fell |

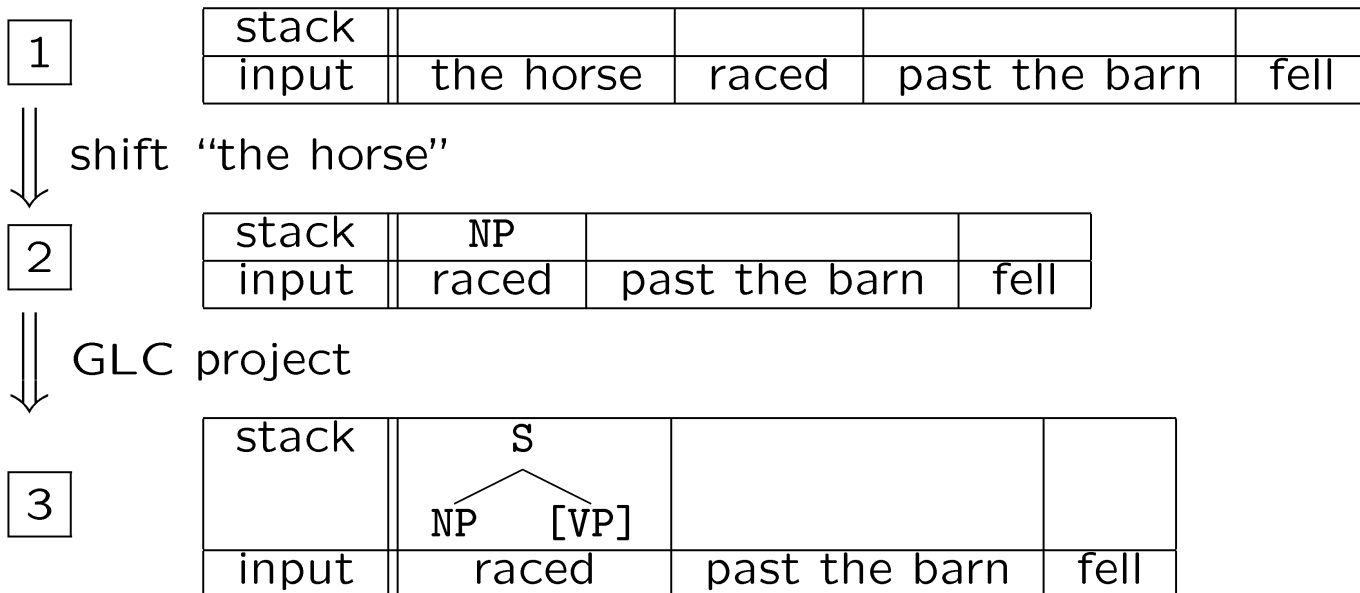
↓ shift "the horse"

| | | | | |
|---|-------|-------|---------------|------|
| 2 | stack | NP | | |
| | input | raced | past the barn | fell |

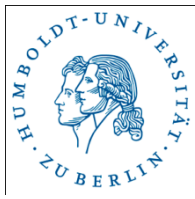
Generalized Left-Corner Parser



The horse raced past the barn fell.



Generalized Left-Corner Parser



The horse raced past the barn fell.

| | | | | | |
|---|-------|-----------|-------|---------------|------|
| 1 | stack | | | | |
| | input | the horse | raced | past the barn | fell |

⇓ shift "the horse"

| | | | | | |
|---|-------|-------|---------------|------|--|
| 2 | stack | NP | | | |
| | input | raced | past the barn | fell | |

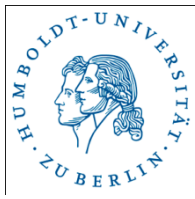
⇓ GLC project

| | | | | | |
|---|-------|-------------------------|---------------|------|--|
| 3 | stack | S ├── NP └── [VP] | | | |
| | input | raced | past the barn | fell | |

⇓ shift "raced"

| | | | | | |
|---|-------|-------------------------|------|---|--|
| 4 | stack | S ├── NP └── [VP] | | V | |
| | input | past the barn | fell | | |

Generalized Left-Corner Parser



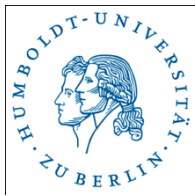
The horse raced past the barn fell.

↓ GLC project

5

| | | |
|-------|---|---|
| stack | $\begin{array}{c} \text{S} \\ \swarrow \quad \searrow \\ \text{NP} \quad [\text{VP}] \end{array}$ | $\begin{array}{c} \text{VP} \\ \swarrow \quad \searrow \\ \text{V} \quad [\text{PP}] \end{array}$ |
| input | past the barn | fell |

Generalized Left-Corner Parser



The horse raced past the barn fell.

↓ GLC project

5

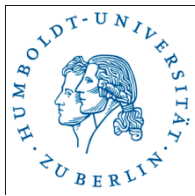
| | | |
|-------|--|--|
| stack | <pre>graph TD S --> NP S --> VP1[VP] NP --> past NP --> the NP --> barn VP1 --> V VP1 --> PP1[PP] V --> fell</pre> | <pre>graph TD VP --> V VP --> PP V --> fell</pre> |
| input | past the barn | fell |

↓ GLC complete

6

| | | |
|-------|--|------|
| stack | <pre>graph TD S --> NP S --> VP NP --> past NP --> the NP --> barn VP --> V VP --> PP V --> fell</pre> | |
| input | past the barn | fell |

Generalized Left-Corner Parser



The horse raced past the barn fell.

↓ GLC project

| | | | | | |
|---|-------|---------------|------|------|------|
| 5 | stack | S | | VP | |
| | | NP | [VP] | V | [PP] |
| | input | past the barn | | fell | |

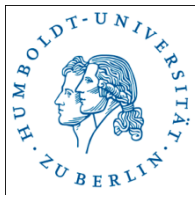
↓ GLC complete

| | | | | |
|---|-------|---------------|----|------|
| 6 | stack | S | | |
| | | NP | VP | |
| | | | V | [PP] |
| | input | past the barn | | fell |

↓ shift "past the barn"

| | | | | |
|---|-------|------|----|------|
| 7 | stack | S | | PP |
| | | NP | VP | |
| | | | V | [PP] |
| | input | fell | | |

Generalized Left-Corner Parser



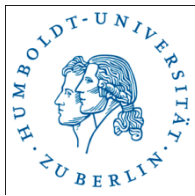
The horse raced past the barn fell.

⇓ GLC complete

8

| | |
|-------|--|
| stack | <pre>graph TD S --> NP S --> VP VP --> V VP --> PP</pre> |
| input | fell |

Generalized Left-Corner Parser



The horse raced past the barn fell.

⇓ GLC complete

8

| | | |
|-------|------|------|
| stack | S | |
| | NP | VP |
| | | V PP |
| input | fell | |

⇓ shift "fell"

9

| | | |
|-------|----|------|
| stack | S | VP |
| | NP | VP |
| | | V PP |
| input | | # |

symptom

Diagnosis

The horse raced past the barn **fell**.

The horse raced past. The barn fell.

?

Lexicon:

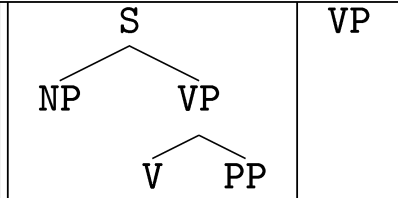
raced = (1) finite verb, past tense

raced = (2) non-finite verb, participle past perfect

Repair

The horse raced past the barn fell.

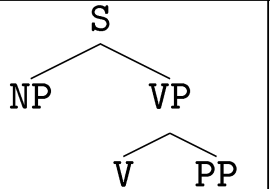
9

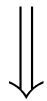
| | | |
|-------|--|----|
| stack |  | VP |
| input | | |

Repair

The horse raced past the barn fell.

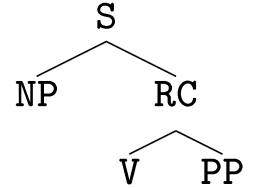
9

| | | |
|-------|---|----|
| stack |  | VP |
| input | | |



repair: replace VP by RC

17

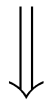
| | | |
|-------|---|----|
| stack |  | VP |
| input | | |

Repair

The horse raced past the barn fell.

9

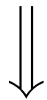
| | | |
|-------|---|----|
| stack | <pre> S / \ NP VP / \ V PP </pre> | VP |
| input | | |



repair: replace VP by RC

17

| | | |
|-------|---|----|
| stack | <pre> S / \ NP RC / \ V PP </pre> | VP |
| input | | |



repair: replace S by NP

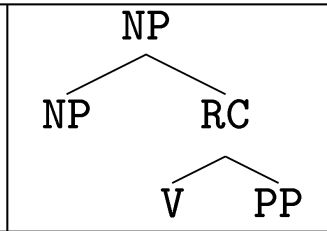
15

| | | |
|-------|--|----|
| stack | <pre> NP / \ NP RC / \ V PP </pre> | VP |
| input | | |

Reanalysis

The horse raced past the barn fell.

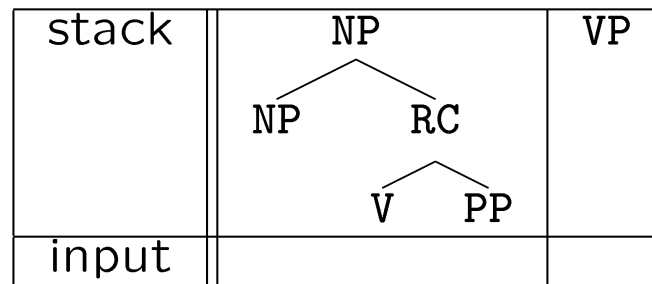
15

| | | |
|-------|--|----|
| stack |  | VP |
| input | | |

Reanalysis

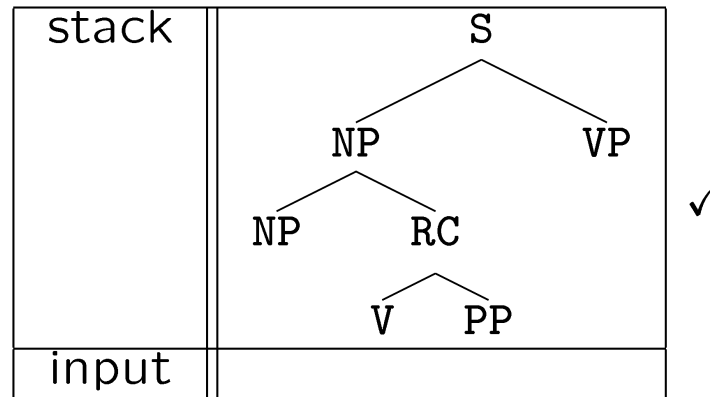
The horse raced past the barn fell.

15

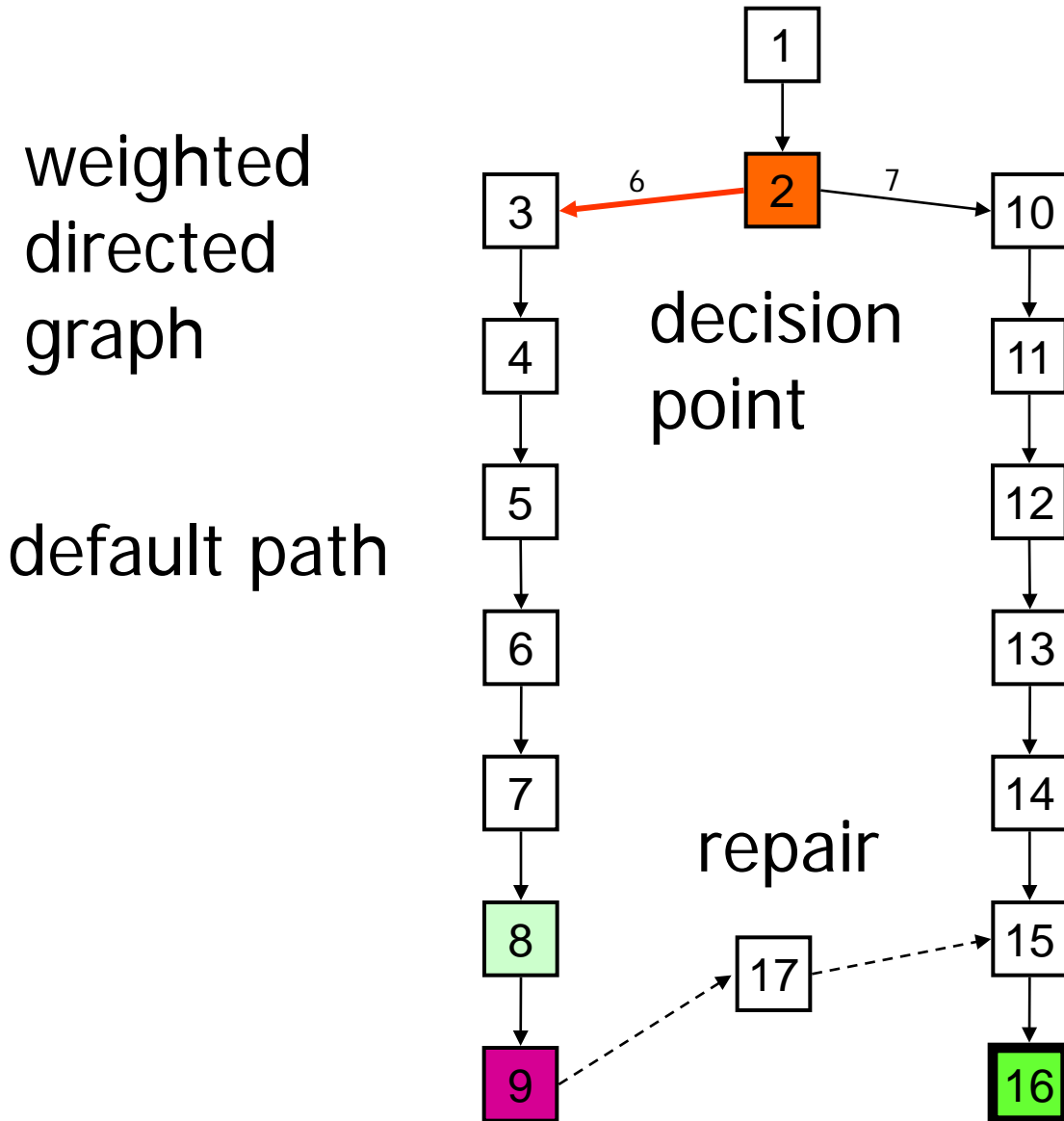


⇓ GLC project

16

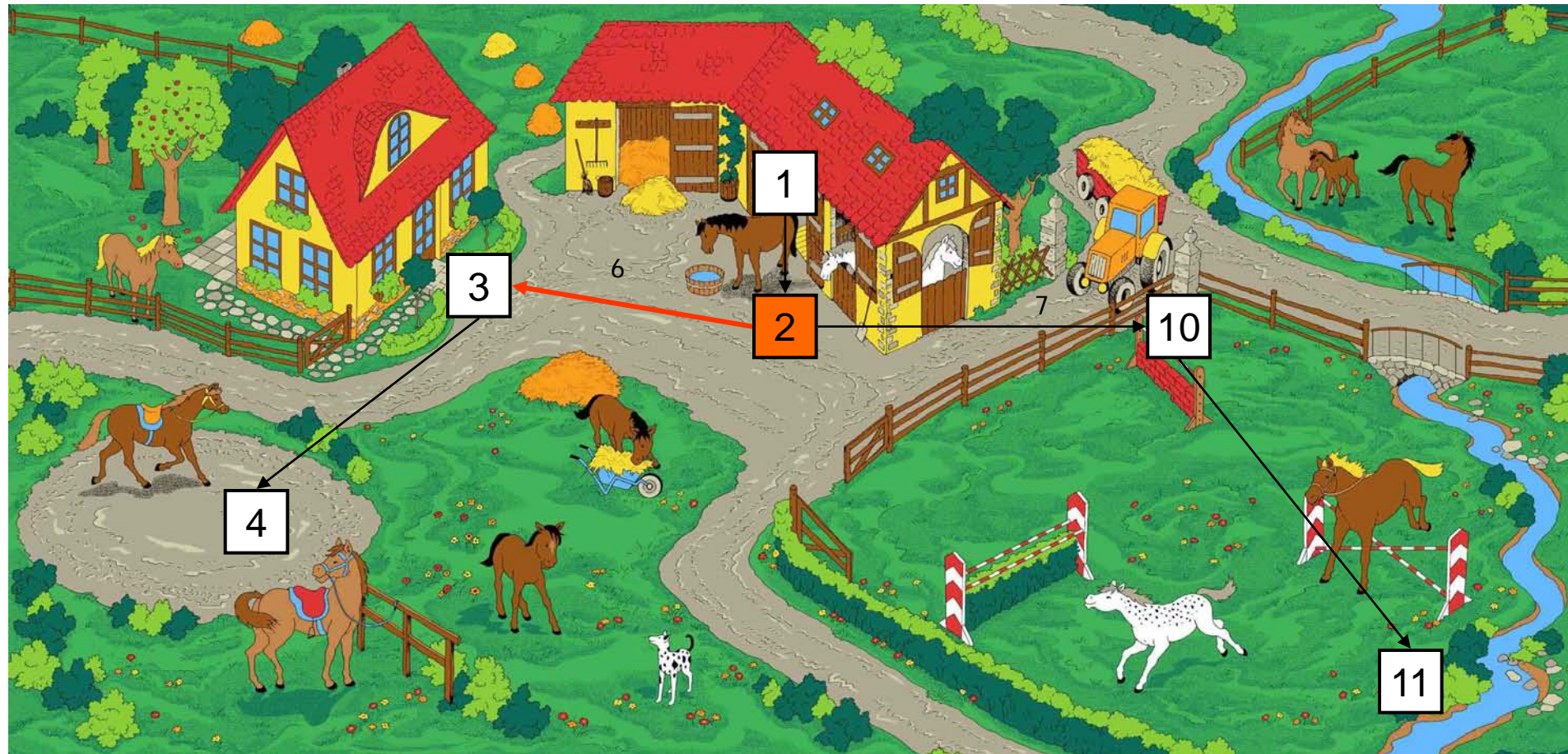


Search Space



A* search:
arrive rapidly!

Geometric Representation



embedding into Euclidian space

Weights

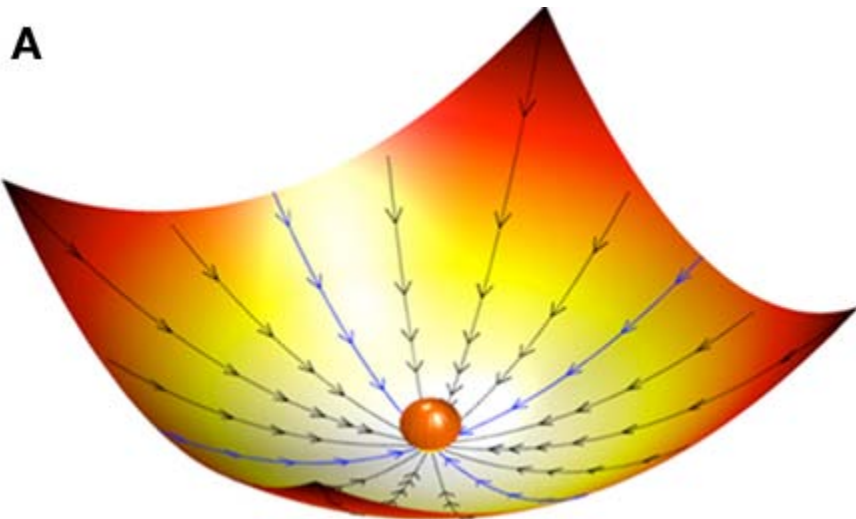
in Euclidian geometry, arc weights could become

1. distances
2. transition times

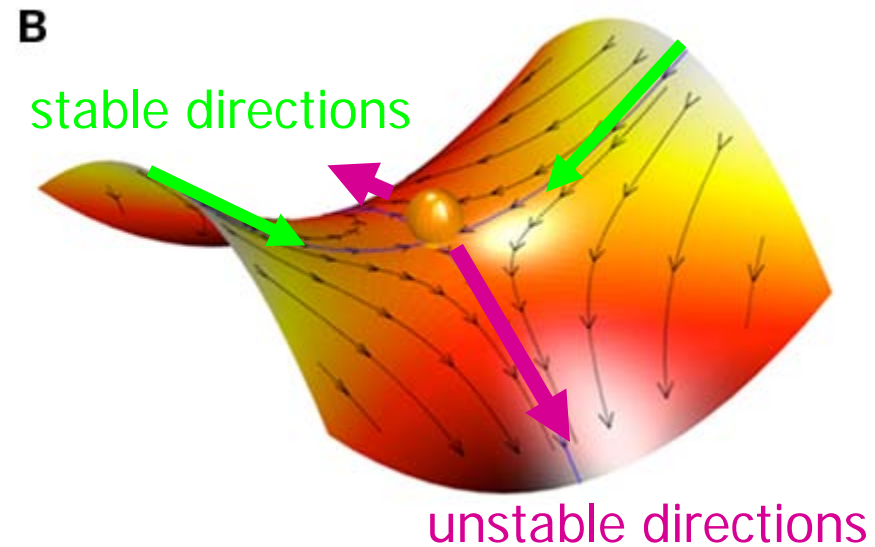
only for constant velocity, 1. and 2. are equivalent

Dynamics

identify parser states with equilibrium points in geometric space



fixed point attractor



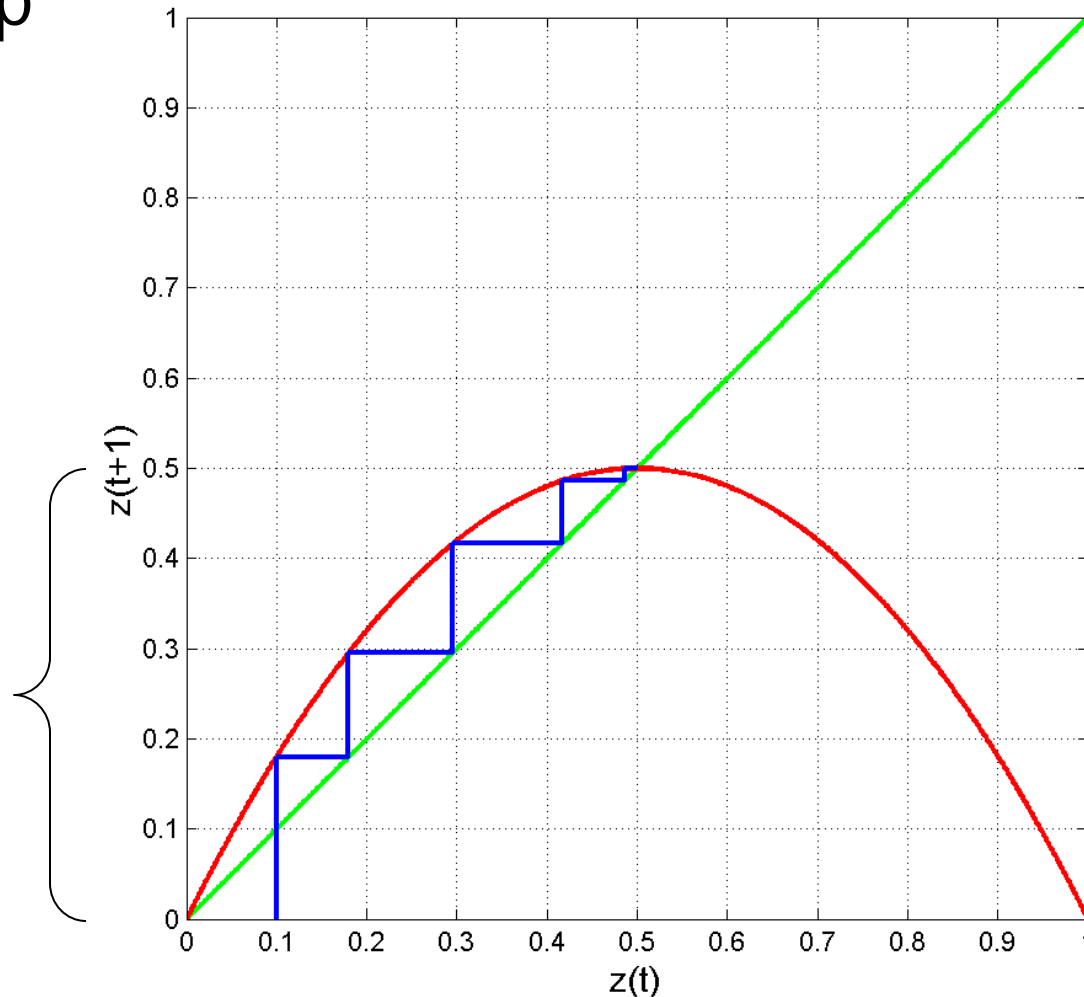
saddle node

Example

logistic map

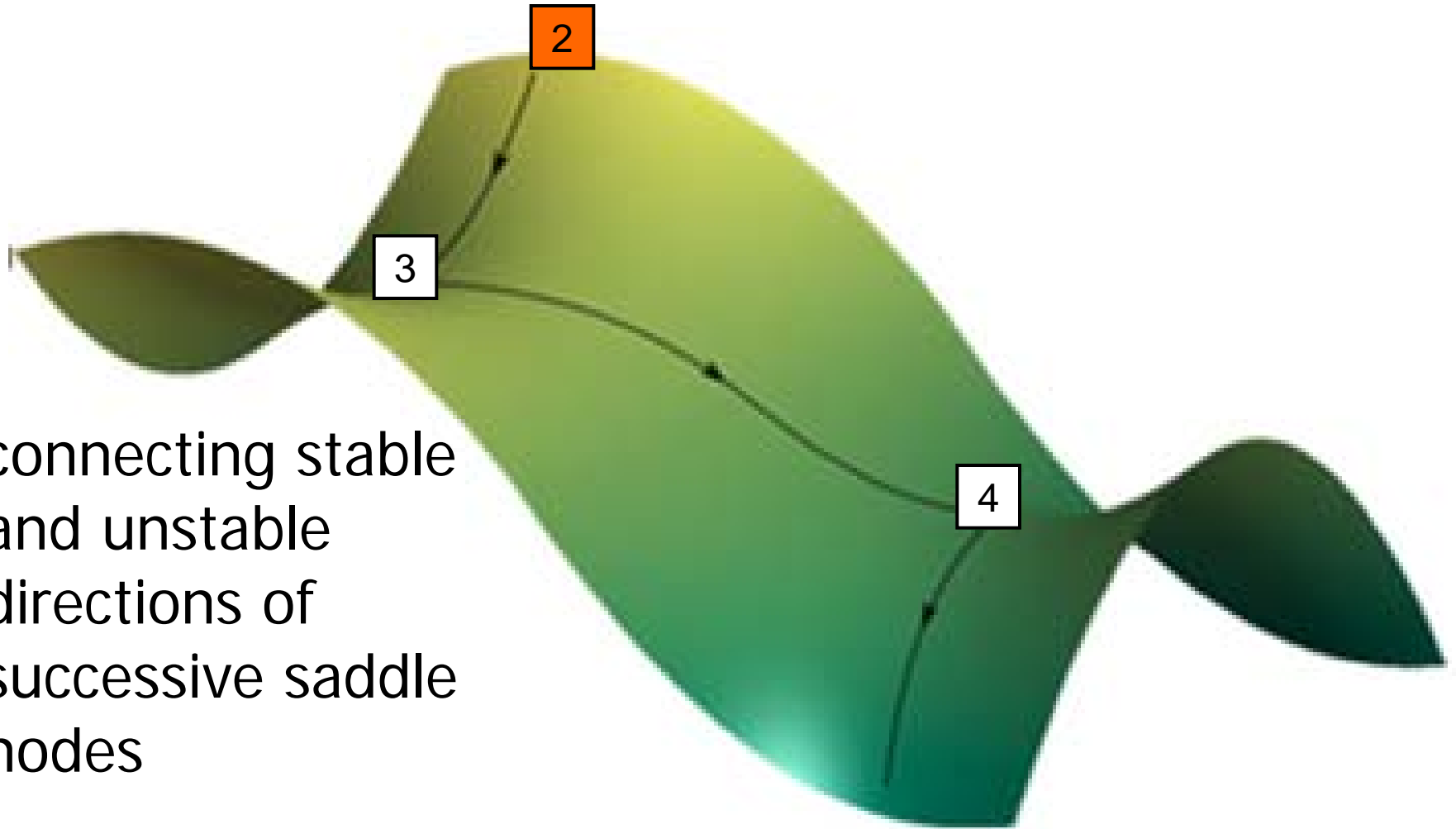
fixed point attractor

control
parameter r



$$z(t+1) = rz(t)(1-z(t))$$

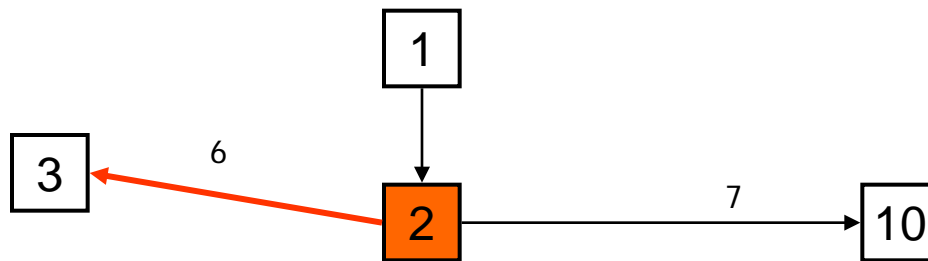
Sequential Dynamics



connecting stable
and unstable
directions of
successive saddle
nodes

stable heteroclinic sequence
(SHS)

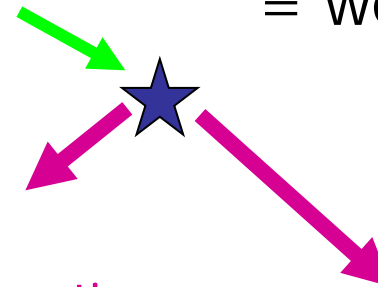
Sequential Decision Problems



stable direction

saddle node with more than one unstable direction
($d > 2$)

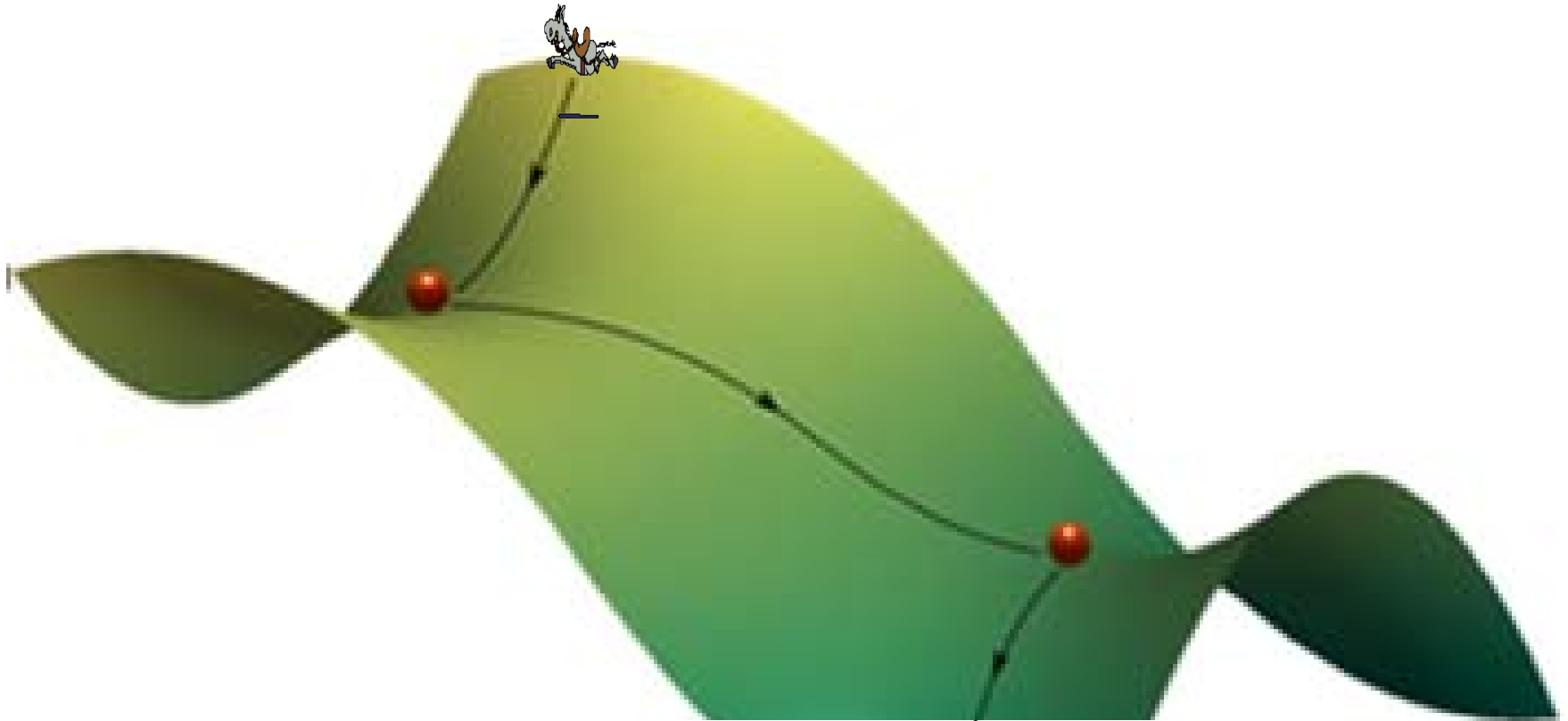
arrow lengths =
escape velocities
= weights



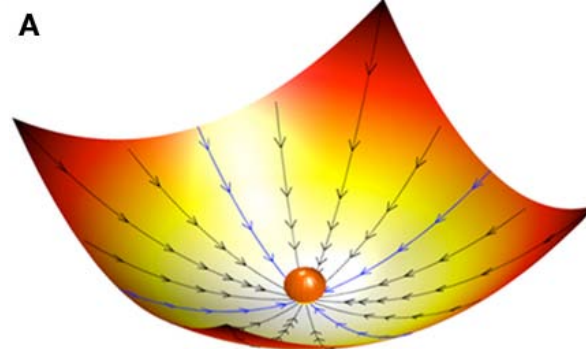
unstable directions

A^* search = high risk decision for large velocities

Gardenpath States



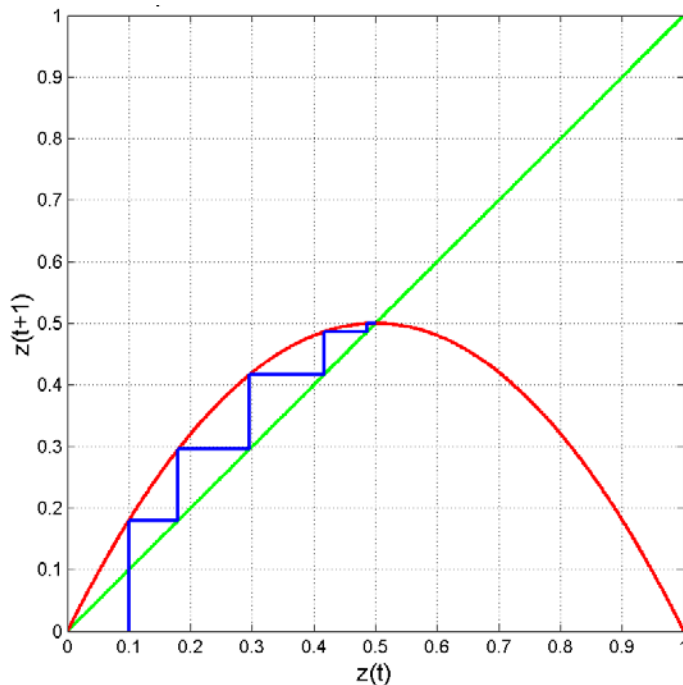
A



unwanted
attractor

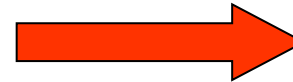
Bifurcations

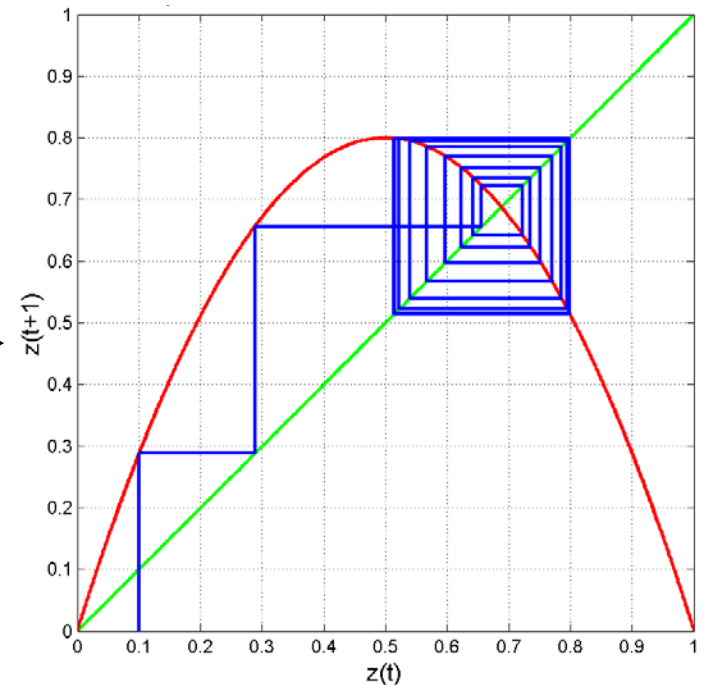
fixed point attractor



$$|F'(z^*)| < 1$$

unstable fixed point

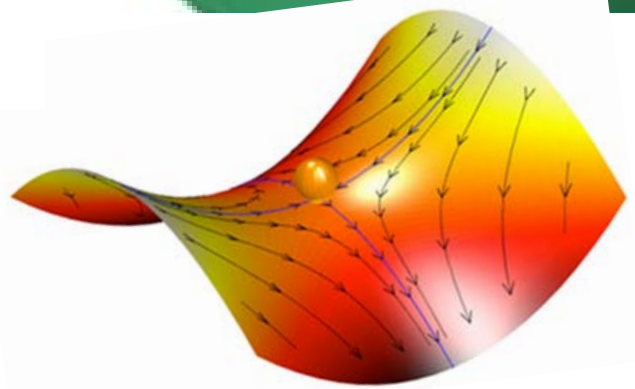
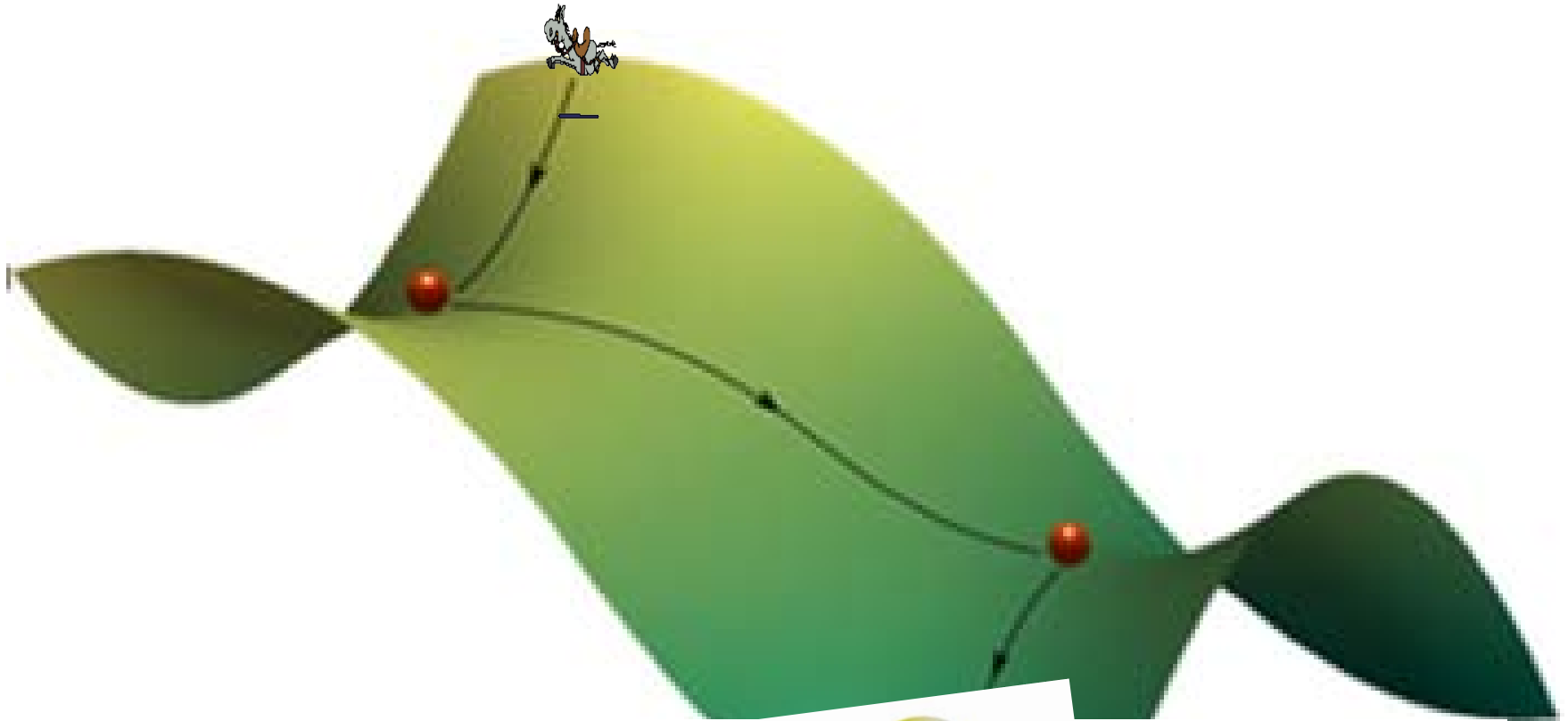
increasing r




$$|F'(z^*)| > 1$$

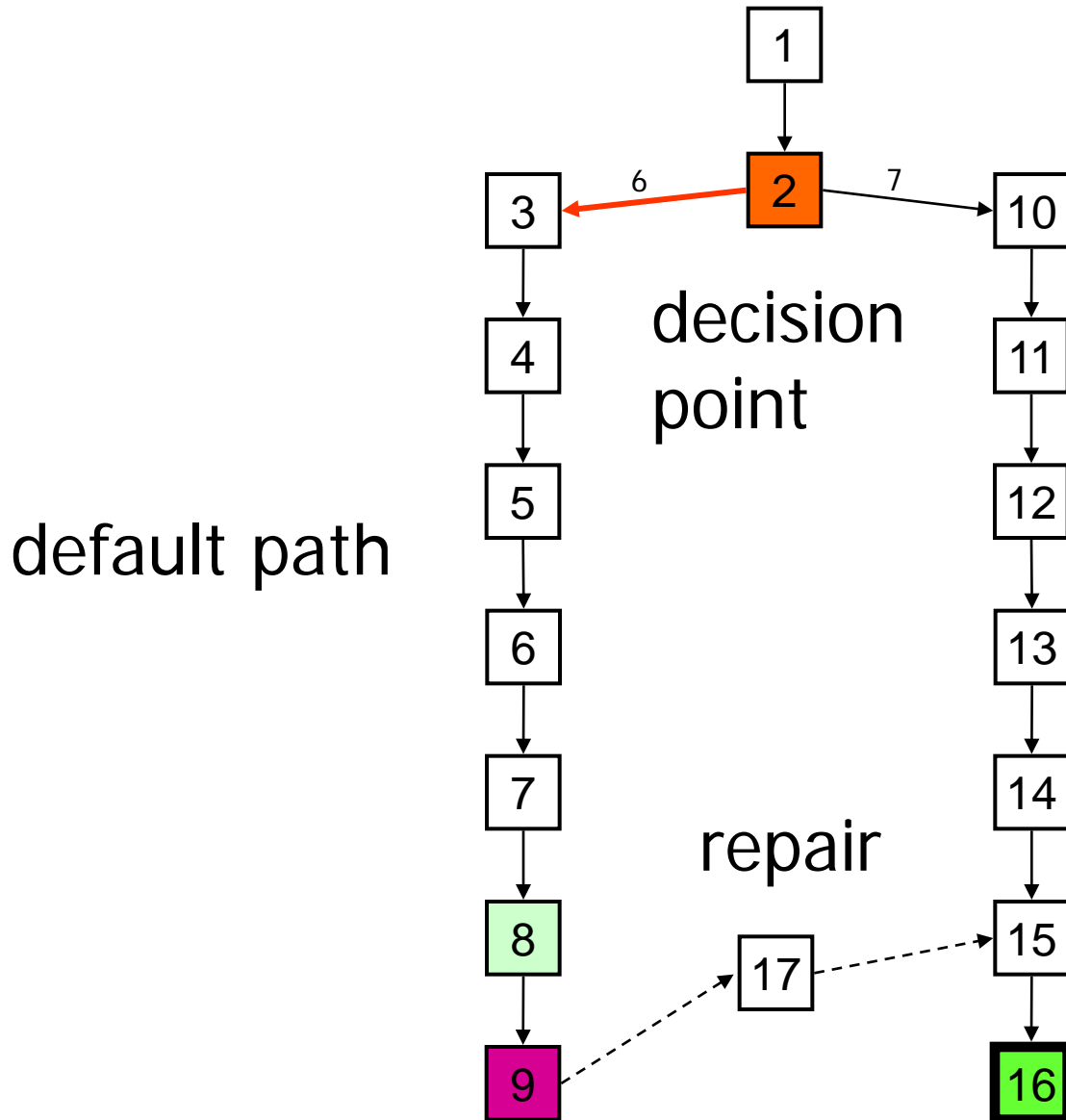
$$z(t + 1) = rz(t)(1 - z(t))$$

Repair by Bifurcation



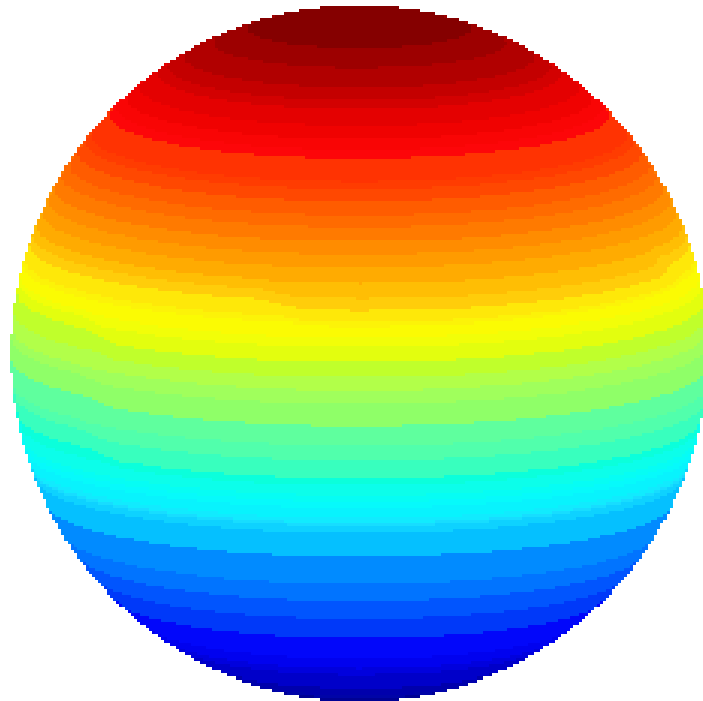
beim Graben et al. (2004)

Search Space



Dynamic Field Parser

The horse raced past the barn fell.



'the horse'

Conclusion

- Syntactic parsing represented by sequential dynamics in geometric space
- Intermediate representational states as saddle nodes connected through stable heteroclinic sequences
- Gardenpath states as unwanted attractors
- A* search as high risk sequential decision strategy
- Syntactic repair as bifurcation of SHS

Acknowledgements

Thank you for your attention!

Funding: DFG Heisenberg-Stipendium GR 3711/1-1

